

# Thriving in Between Theory and Practice: How Applied Cryptography Bridges the Gap

---

**Matilda Backendal**

Applied Cryptography Group  
ETH Zurich

&

**Miro Haller**

Computer Science and Engineering  
University of California, San Diego



**ETH** zürich

UC San Diego

NIST Crypto Reading Club, April 3, 2024

# CAW: Cryptographic Applications Workshop



26TH MAY 2024  
EUROCRYPT 2024 AFFILIATED EVENT

## CRYPTOGRAPHIC APPLICATIONS WORKSHOP

1. Formalizing the security of deployed cryptography. **PROOFS**
2. Constructing cryptographic primitives and systems for practice. **DESIGN**
3. The industry perspective on deployment and maintenance of cryptography. **"PRACTICE"**

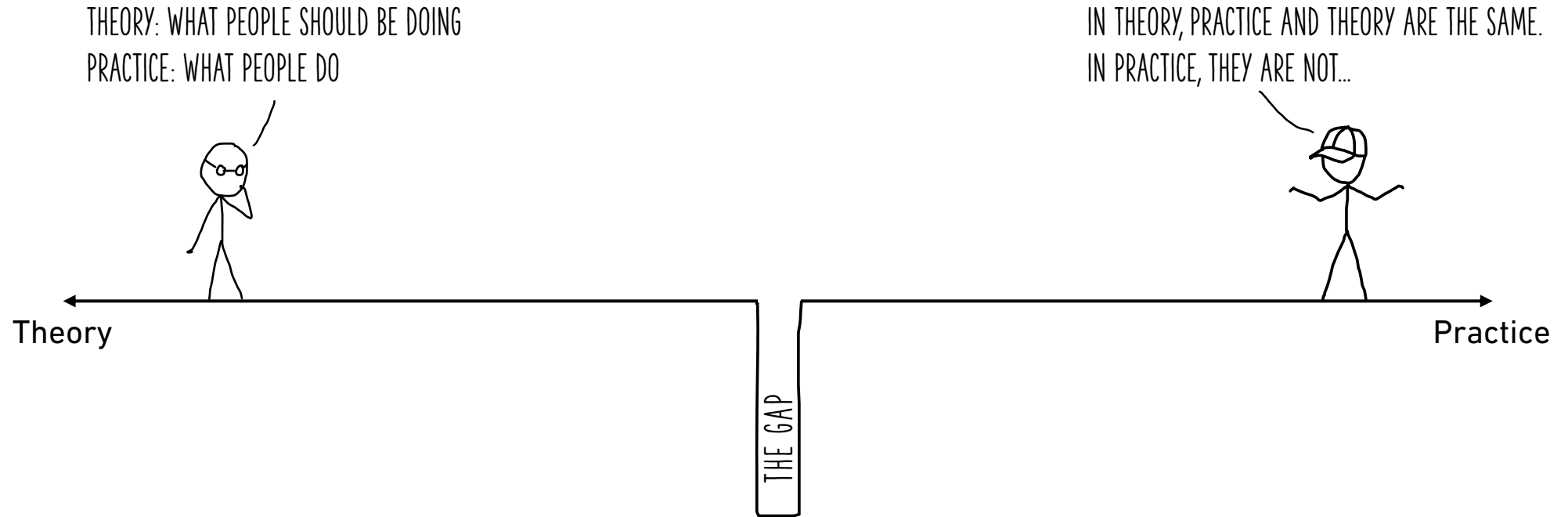
# CAW: Cryptographic Applications Workshop

More on  
[caw.cryptanalysis.fun](http://caw.cryptanalysis.fun)

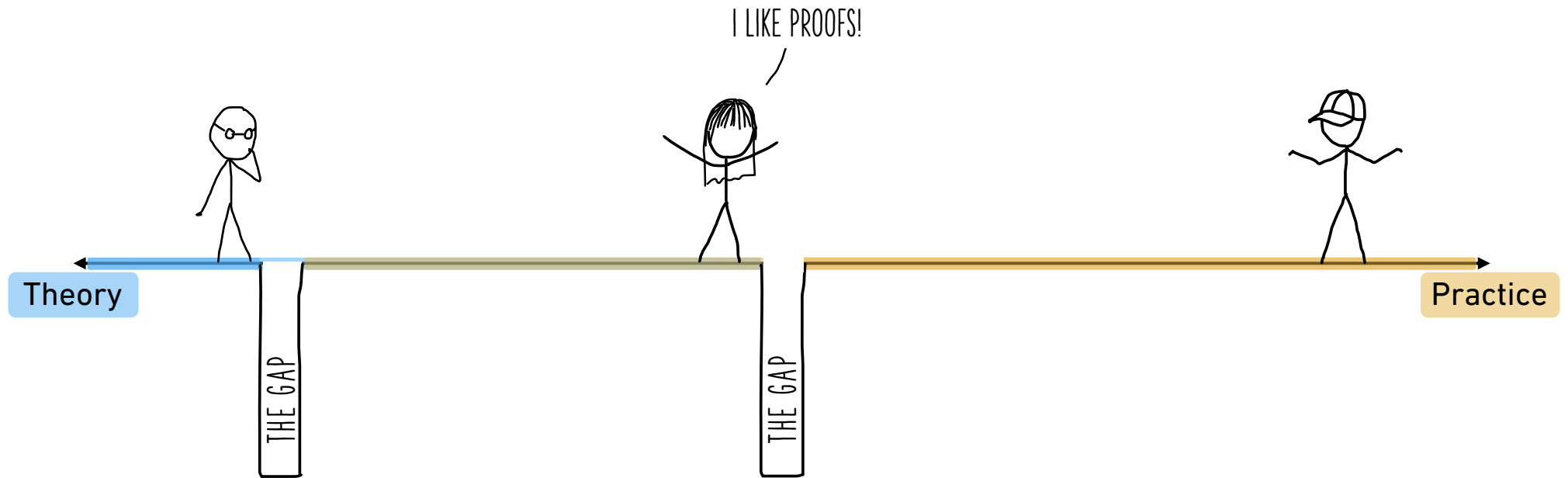
Sunday, May 26 2024		
9:10–9:35 (CEST)	"Practical Private Information Retrieval for Real Databases" by <b>Sofía Celi, Alex Davidson</b>	✓
9:35–10:00 (CEST)	"How to Encrypt a File at Scale" by <b>Moreno Ambrosin, Fernando Lobato Meeser</b>	✓
10:00–10:30 (CEST)	"Analyzing Cryptography in Context: The Case Study of Apple's CSAM Scanning Proposal" by <b>Gabriel Kaptchuk</b>	✓
11:00–11:45 (CEST)	"Why we can't have nice (cryptographic) things" by <b>Henry Corrigan-Gibbs</b> (invited speaker)	✓
11:45–12:30 (CEST)	"Recent Results on Group Messaging (title TBD)" by <b>Daniel Collins, Phillip Gajland, Paul Rösler</b>	✓
13:30–14:00 (CEST)	"Securing semi-open group messaging" by <b>Fernando Virdia</b>	✓
14:00–14:30 (CEST)	"A Computational Security Analysis of Signal's PQXDH handshake" by <b>Rune Fiedler</b>	✓
14:30–15:00 (CEST)	"Bytes to schlep? Use a FEP: Hiding Protocol Metadata with Fully Encrypted Protocols" by <b>Aaron Johnson</b>	✓
15:30–16:00 (CEST)	"Computing on your data with MPC" by <b>Christopher Patton</b>	✓
16:00–17:00 (CEST)	Panel on standardization	✓

Standards!

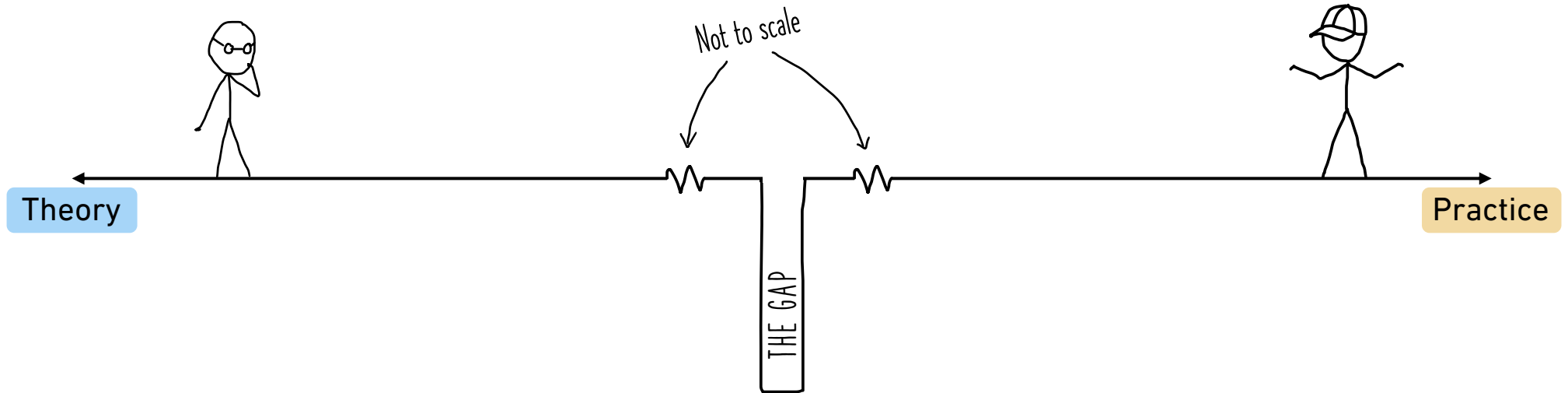
# The Gap



# The Gap



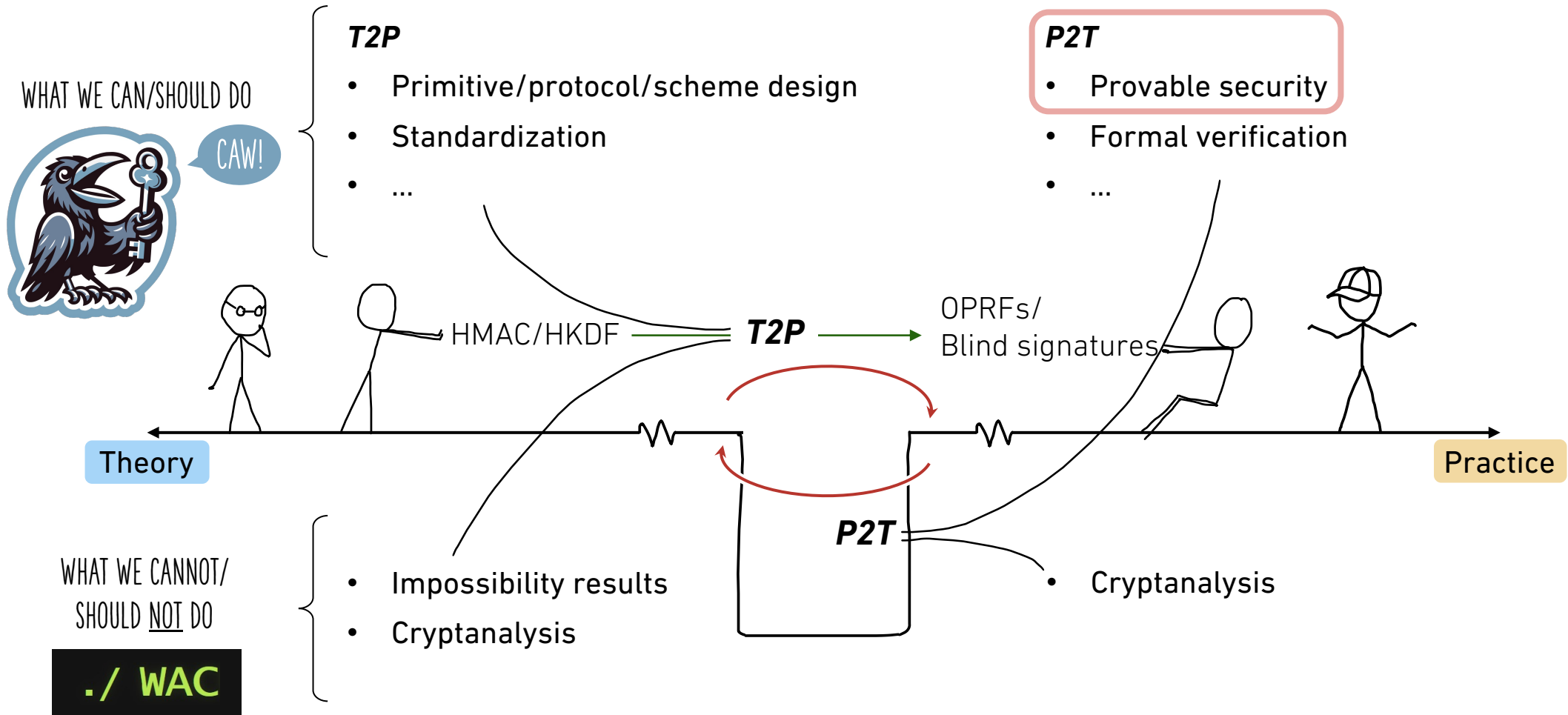
# The Gap



# Taxonomy of Cryptography

	Theory	Practice
Theory	<b><i>T2T</i></b>	<b><i>T2P</i></b>
Practice	<b><i>P2T</i></b>	<b><i>P2P</i></b>

# Bridging the Gap



## Workshop on Attacks in Cryptography



# Dual-PRF Security of HMAC

---

Based on work with Mihir Bellare, Felix Günther & Matteo Scarlata

# HMAC: the Swiss Army Knife of Crypto

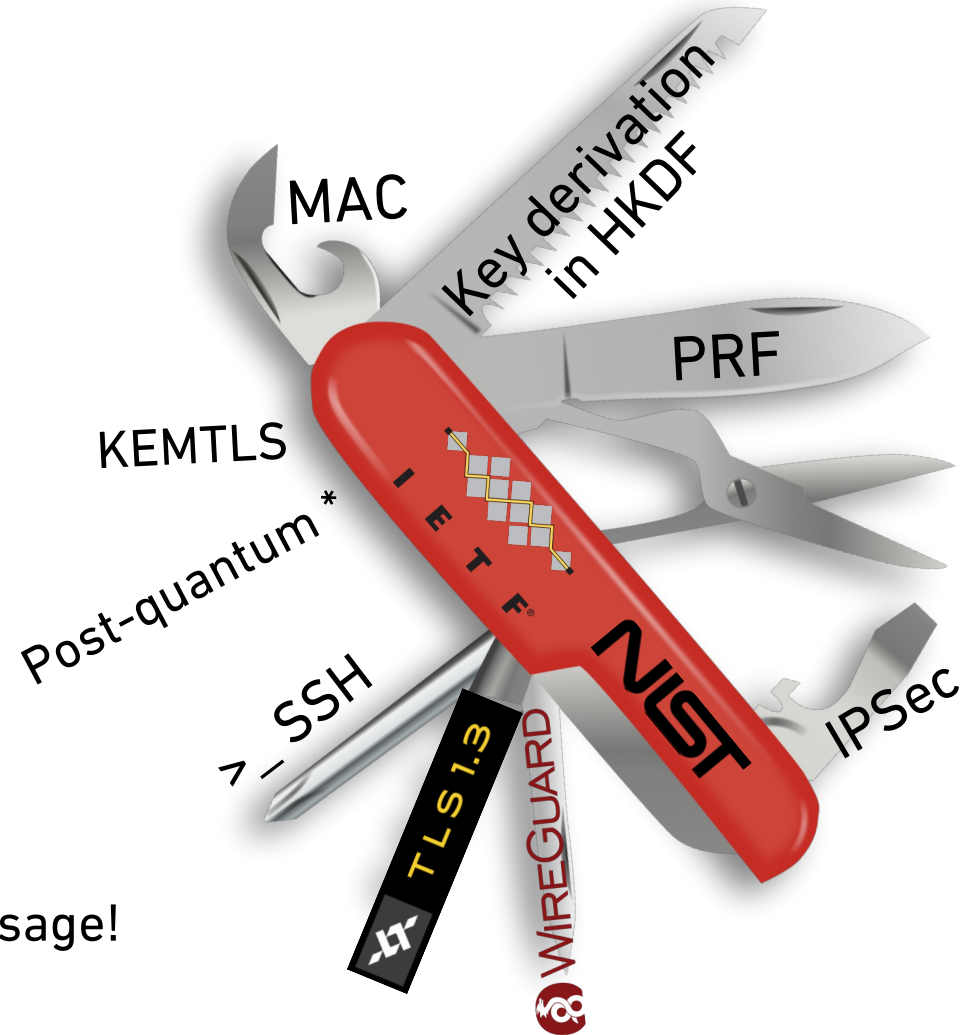
HMAC [CRYPTO'96:BCK] is

- a hash-based MAC,
- standardized,
- provably secure,
- versatile,
- and widely used.

...as a PRF

[C'96:BCK, C'06:Bel, C'14:GPR].

This doesn't match current usage!



# The HMAC Gap

HMAC IS A SECURE PRF



Theory

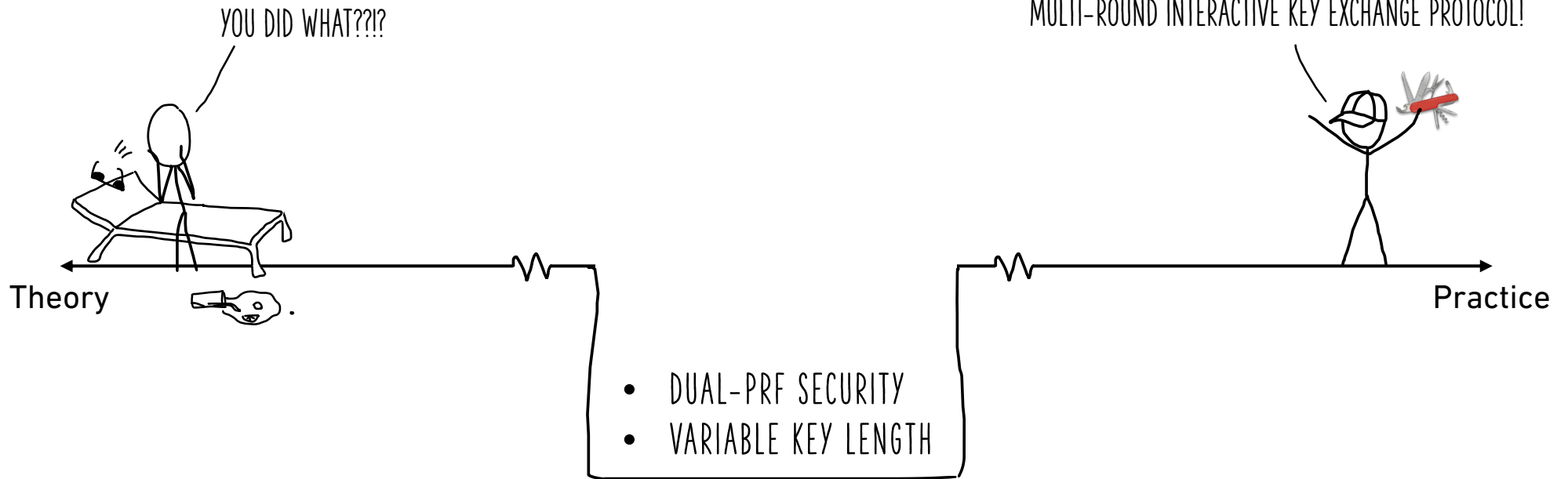
OH WOW, THIS SCISSOR TOOL IS PERFECT FOR MY MULTI-ROUND INTERACTIVE KEY EXCHANGE PROTOCOL!



Practice

- DUAL-PRF SECURITY
- VARIABLE KEY LENGTH

# The HMAC Gap

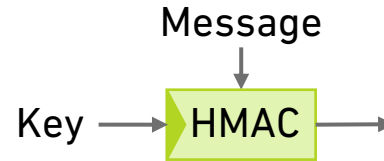


# HMAC in Action

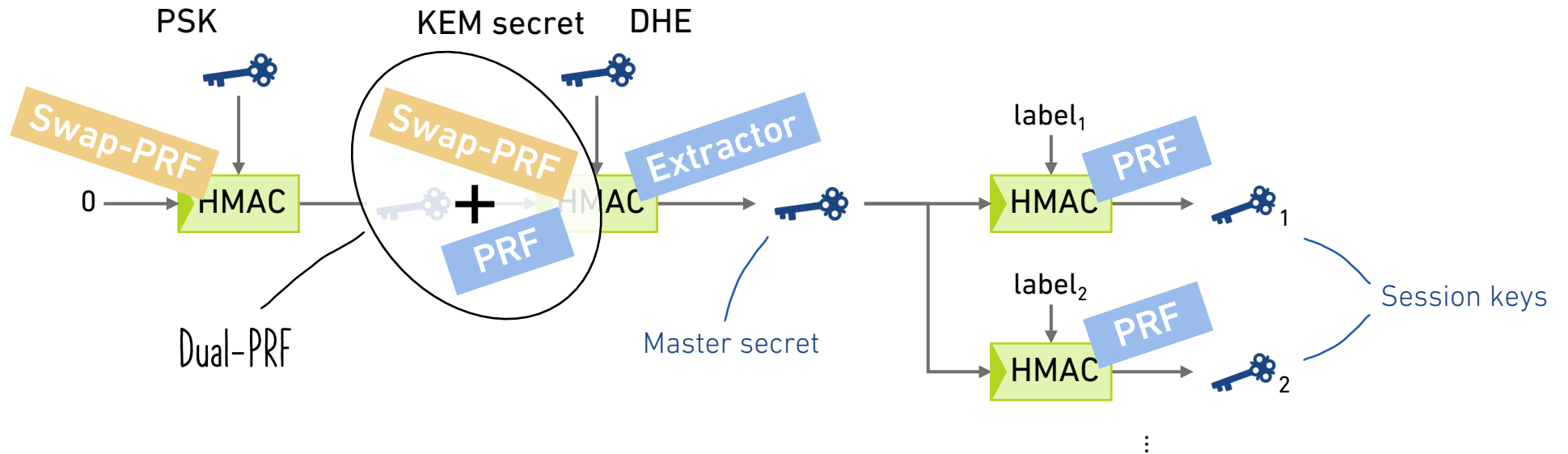
$$\text{HMAC}: \{0,1\}^* \times \{0,1\}^* \rightarrow \{0,1\}^c$$

Key space    Message space

Variable key length



## TLS 1.3 Key Schedule



# HMAC Is Assumed to Be a Dual-PRF

In the analysis of:

- TLS 1.3 PSK [JoC'22:DFGS]
- KEMTLS [CCS'20:SSW]
- PQ Wireguard [S&P'21:HNSWZ]
- PQ Noise [CCS'22:ADHSW]
- Messaging Layer Security (MLS) [S&P'22:BCK]

THEOREM 4.1. Let  $\mathcal{A}$  be an algorithm, and let  $n_s$  be the number of sessions and  $n_u$  be the number of parties. Then the advantage of  $\mathcal{A}$  in breaking the multi-stage security of KEMTLS is upper-bounded by

$$\frac{n_s^2}{2^{|\text{nonce}|}} \left( n_s \left( \epsilon_{\text{KEM}_e}^{\text{IND-1CCA}} + \epsilon_{\text{HKDF.Ext}}^{\text{PRF-sec}} \right) + 2 \epsilon_{\text{HKDF.Ext}}^{\text{dual-PRF-sec}} + 3 \epsilon_{\text{HKDF.Exp}}^{\text{PRF-sec}} \right)$$

The first assumption is concerned with the use of HMAC as a dual PRF (cf. [Bel ...])

**Theorem 6.2** (Multi-Stage security of TLS1.3-PSK-ORTT). *The TLS 1.3 PSK 0-RTT is Multi-Stage-secure with properties (M, AUTH, FS, USE, REPLAY) given above. Formally, for any efficient adversary  $\mathcal{A}$  against the Multi-Stage security there exist efficient algorithms  $\mathcal{B}_1, \dots, \mathcal{B}_8$  such that*

$$\left( \text{Adv}_{\text{KEMTLS}}^{\text{Multi-Stage}}(\mathcal{A}) \leq \left( \text{Adv}_{\text{KEM}_e}^{\text{IND-1CCA}} + \text{Adv}_{\text{HKDF.Ext}}^{\text{PRF-sec}} + \text{Adv}_{\text{HKDF.Ext}}^{\text{dual-PRF-sec}} + \text{Adv}_{\text{HKDF.Exp}}^{\text{PRF-sec}} \right) \right)$$

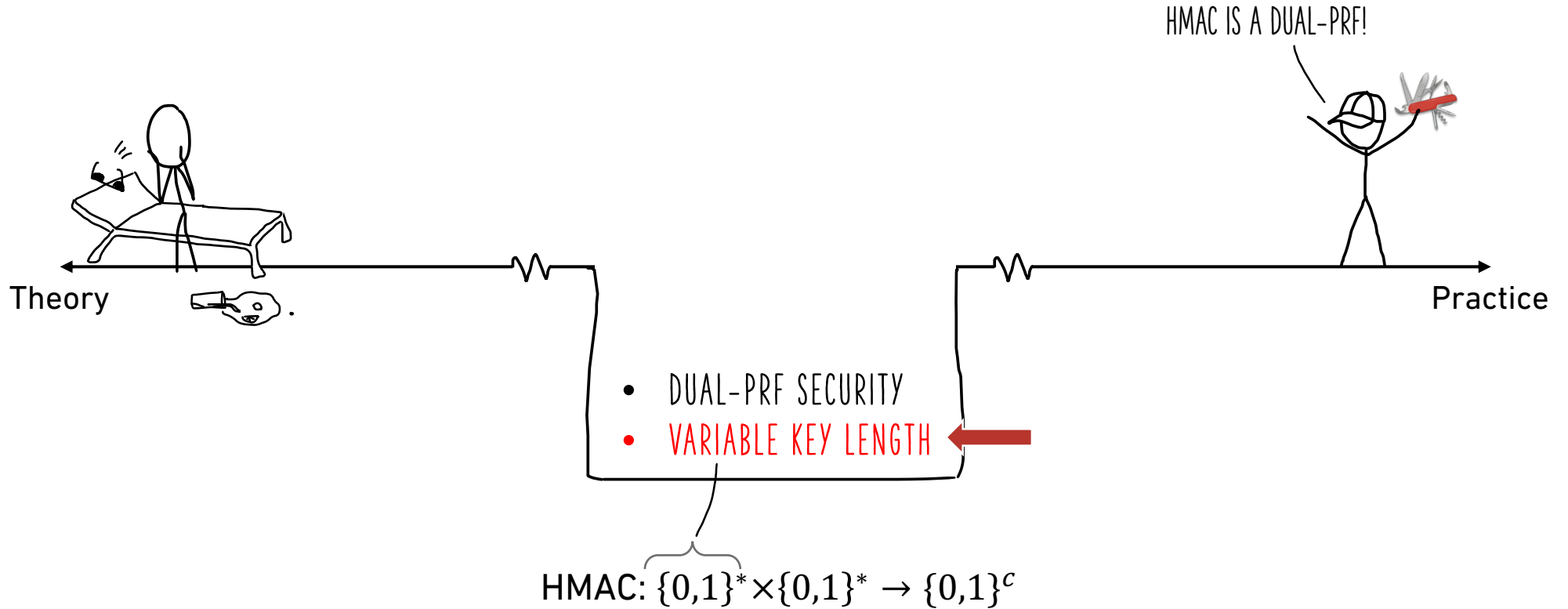
In PQ-WireGuard a dual-PRF appears in the form of a key derivation function  $\text{KDF}(X, Y) = Z$  that takes two inputs,  $X$  and  $Y$ , and outputs a bit string  $Z$  consisting of three blocks  $Z = Z_1 || Z_2 || Z_3$ . We write  $\text{KDF}_i(X, Y)$  for the  $i$ -th block of output of  $\text{KDF}(X, Y)$ , i.e.,  $Z_i$ . The reason why KDF has to be a dual-PRF is discussed in Section IV-A.

**Assumptions.** We make standard key indistinguishability and collision-resistance assumptions on the key derivation functions (KDF) and assume indistinguishability under chosen-ciphertext attacks (IND-CCA) secure public-key encryption, as well as that the Extract function in Krawczyk's HKDF design [24] is a dual pseudorandom function and thus, we assume that HKDF is a dual KDF, which has also been assumed in the analysis of Noise [21] and TLS 1.3 [12].

**Theorem 1.** A Noise Hash Object NHO is a secure pseudo-random Hash-Object if HMAC-HASH is a dual-prf with:  $\text{Adv}_{\text{NHO}, \mathcal{A}, q_i}^{\text{PRHO}}(1^\lambda) \leq \left( \text{Adv}_{\text{HMAC-HASH}, \mathcal{A}'}^{\text{CollRes}}(1^\lambda) + \text{Adv}_{\text{HMAC-HASH}, \mathcal{A}'}^{\text{PRF-SWAP}}(1^\lambda) + (2 \cdot q) \cdot \text{Adv}_{\text{HMAC-HASH}, \mathcal{A}'}^{\text{PRF}}(1^\lambda) \right)$  where  $q$  refers to the total number of oracle-queries.

Appendix A for a proof. Intuitively the security of HMAC-HASH implies that only oracle queries result in equal states and the HMAC-HASH as a dual-PRF (see Appendix B.2) ensures that when added to a chain, its first state becomes the state which is retained upon subsequent calls.

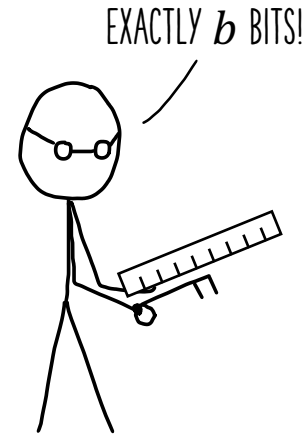
# The HMAC Gap



# HMAC in Action

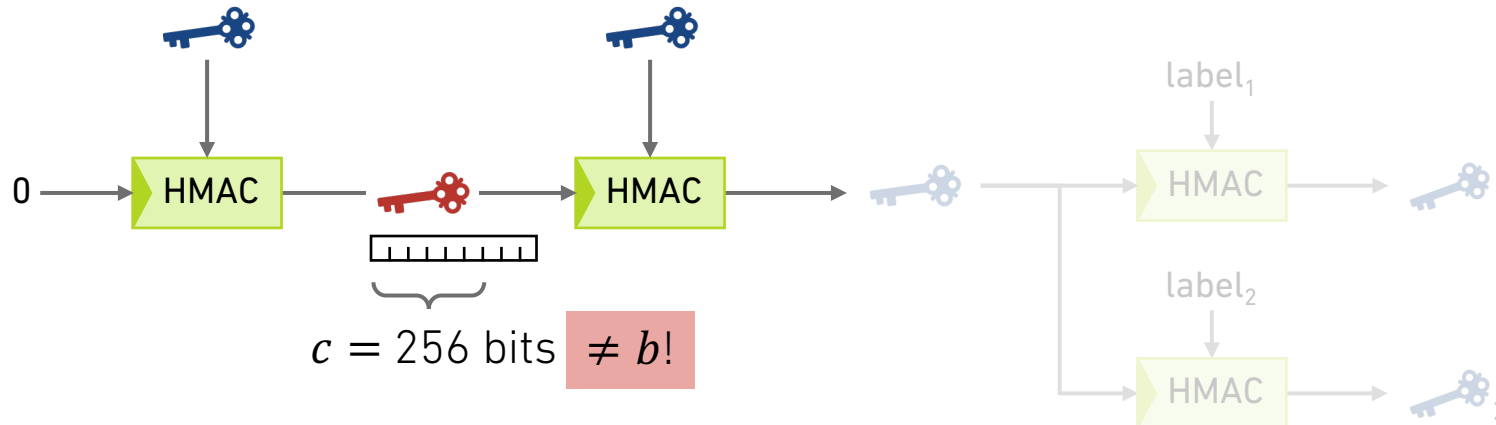
$$\text{HMAC}(K, M) = H((K \oplus \text{opad}) \parallel H((K \oplus \text{ipad}) \parallel M))$$

Merkle-Damgård hash function,  $b$ -bit constants  
e.g. SHA-256:  $c = 256$ ,  $b = 512$



PRF proof:  
 $\text{HMAC}_b(K_b, M)$

## TLS 1.3 Key Schedule





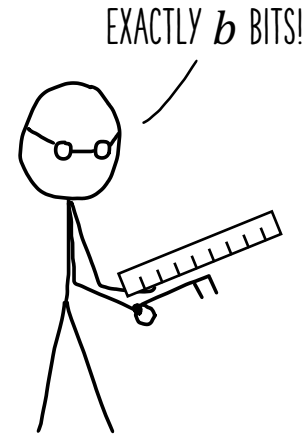
# HMAC in Action

$$\text{HMAC}(K, M) = H((K \oplus \text{opad}) \parallel H((K \oplus \text{ipad}) \parallel M))$$

Pad-or-Hash(K)

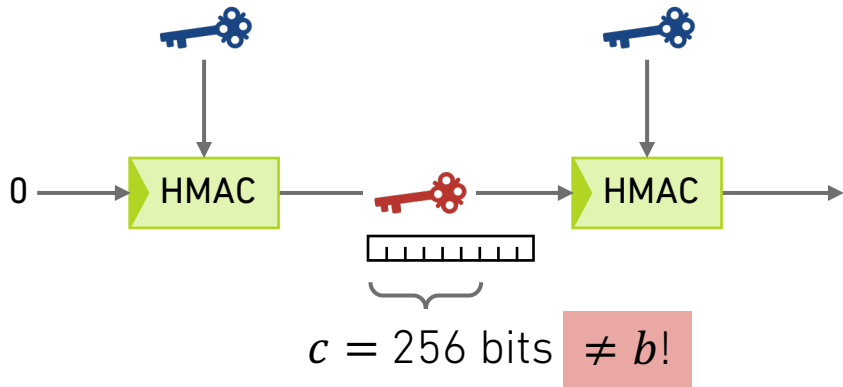


$b$  bits



PRF proof:  
 $\text{HMAC}_b(K_b, M)$

## TLS 1.3 Key Schedule



### Summary

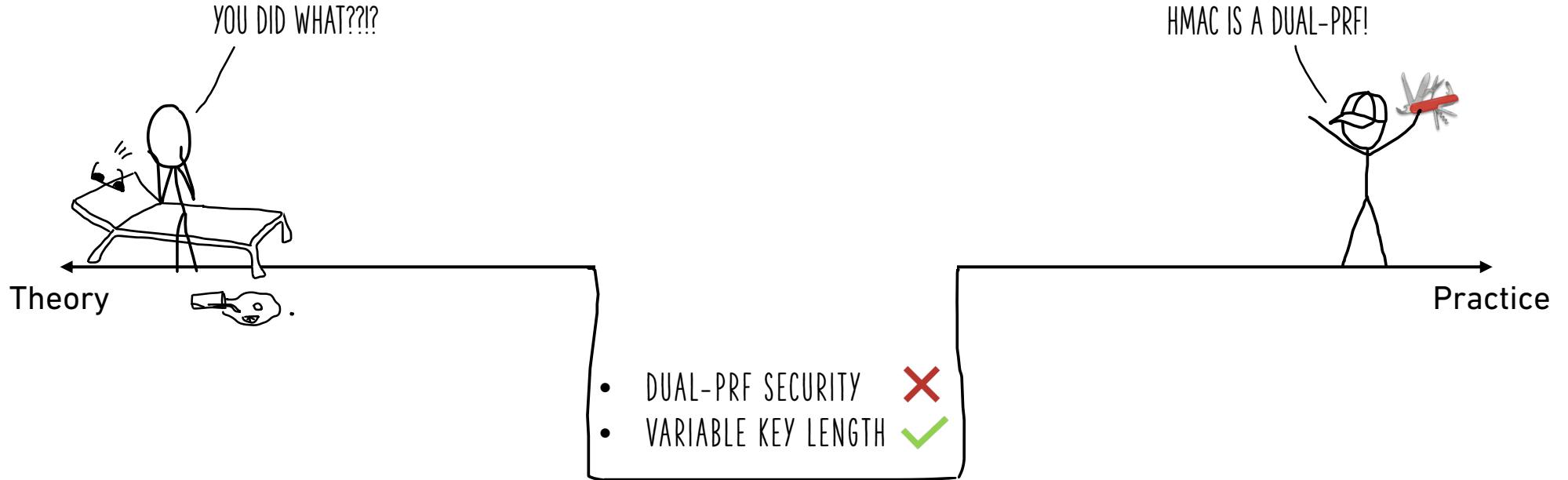
Proof existed:

✓  $\text{HMAC}_b(K_b, M)$

No proof existed:

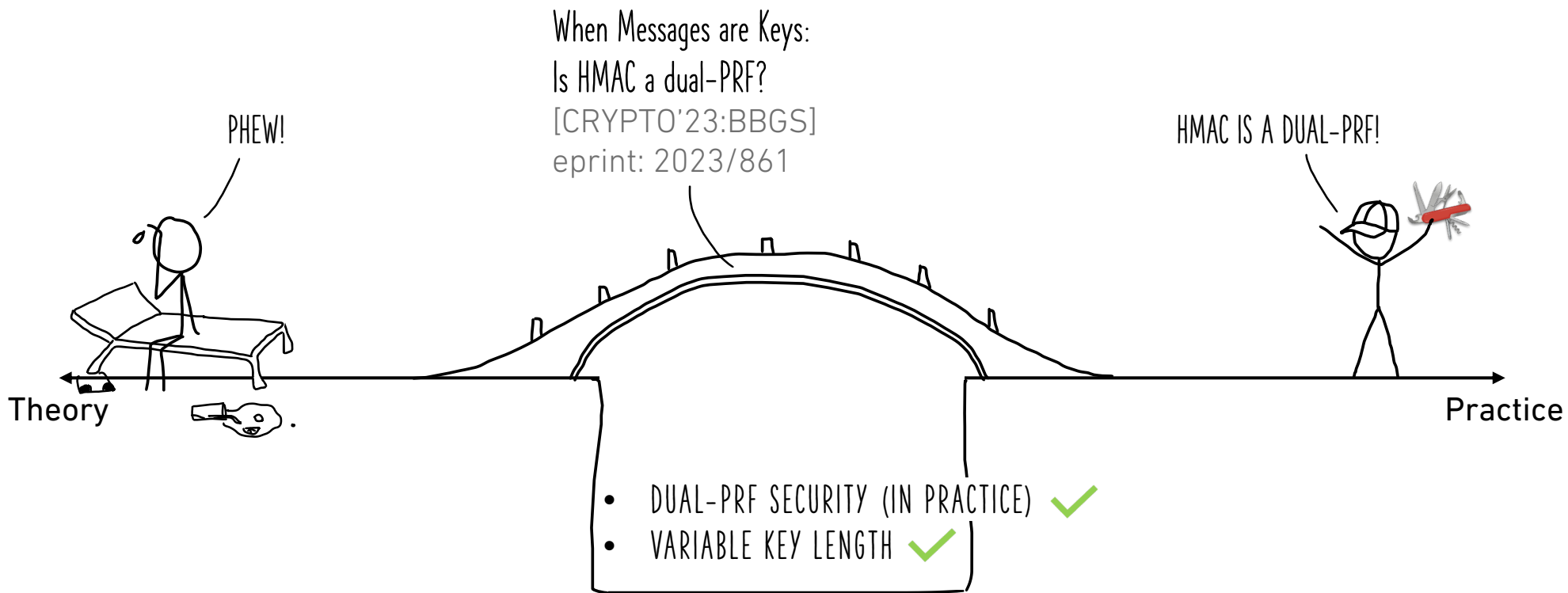
- ✗  $\text{HMAC}(K, M) = H((\text{PoH}(K) \oplus \text{opad}) \parallel H((\text{PoH}(K) \oplus \text{ipad}) \parallel M))$
- ✗  $\text{HMAC}(M, K)$

# The HMAC Gap



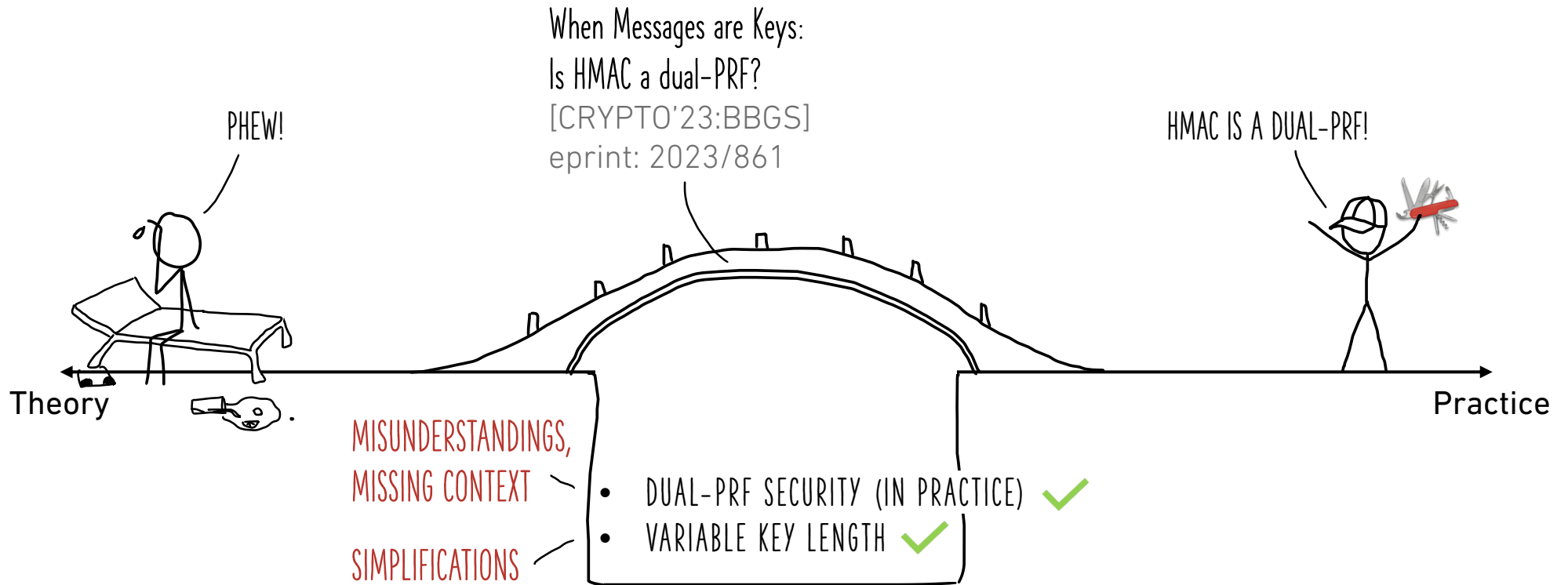
## Is HMAC a Variable-Key Length Dual-PRF?

# The HMAC Gap



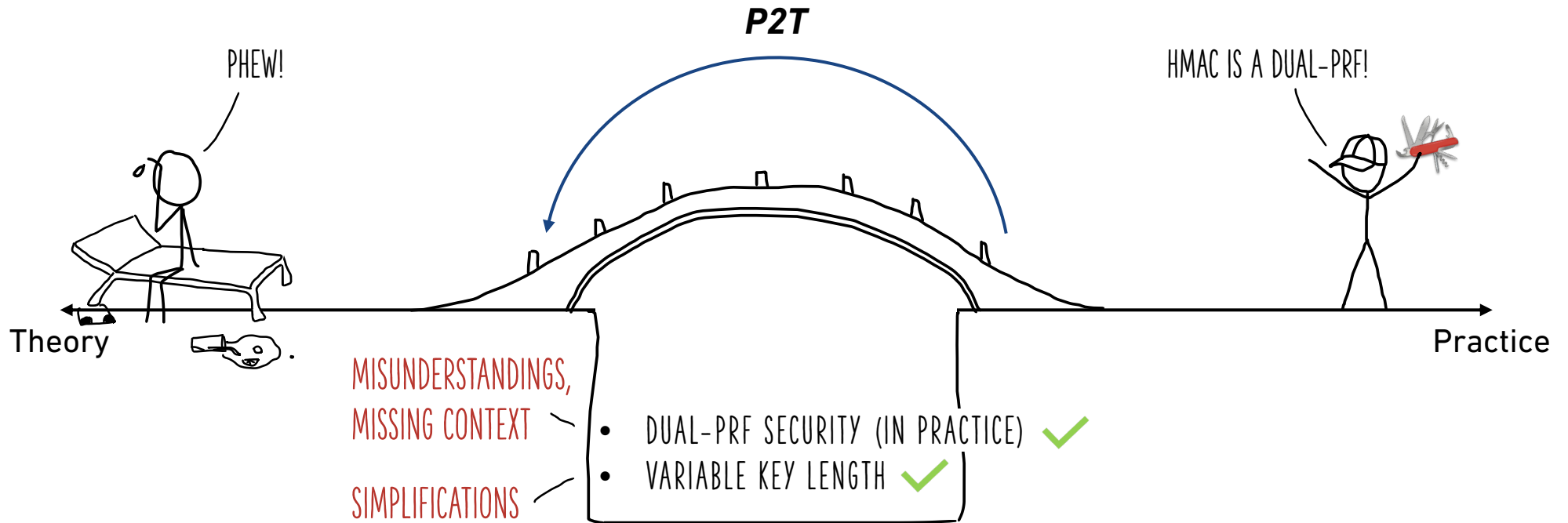
## Is HMAC a Variable-Key Length Dual-PRF?

# The HMAC Gap



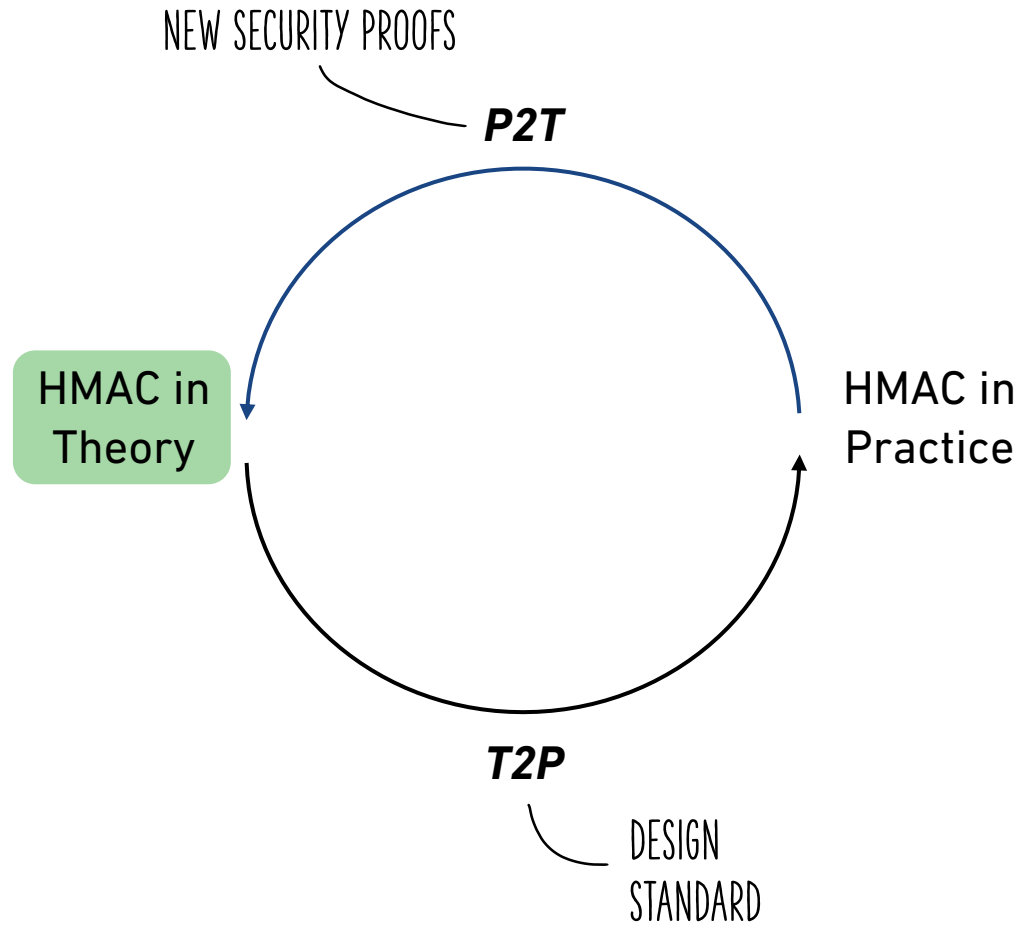
## Why Did the Gap Arise?

# The HMAC Gap



## Why Did the Gap Arise?

# The HMAC Cycle



# End-to-End Encrypted Cloud Storage

---

Based on work with Hannah Davis, Felix Günther & Kenny Paterson

# Why Do We Want E2EE Cloud Storage?

## Privacy

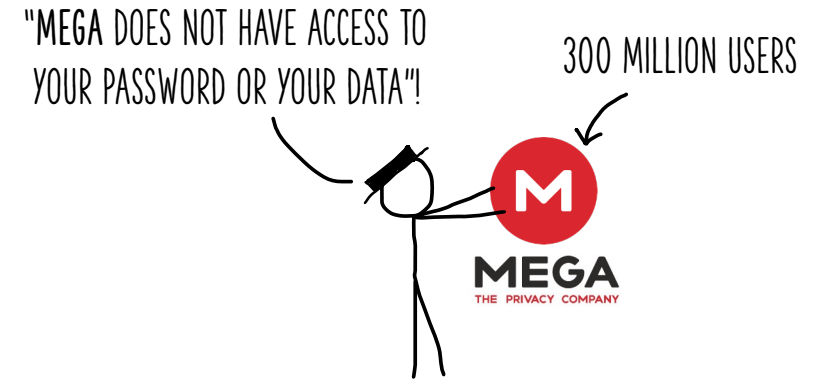
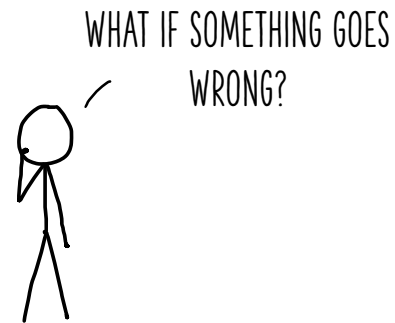
- Sensitive files
- No analytics or data processing

## Security

- Untrusted or compromised provider
- Legally compelled to disclose

## E2EE in other domains

- Data in transit (browsing, messaging)
- Data at rest (local storage, backups)



no E2EE per default

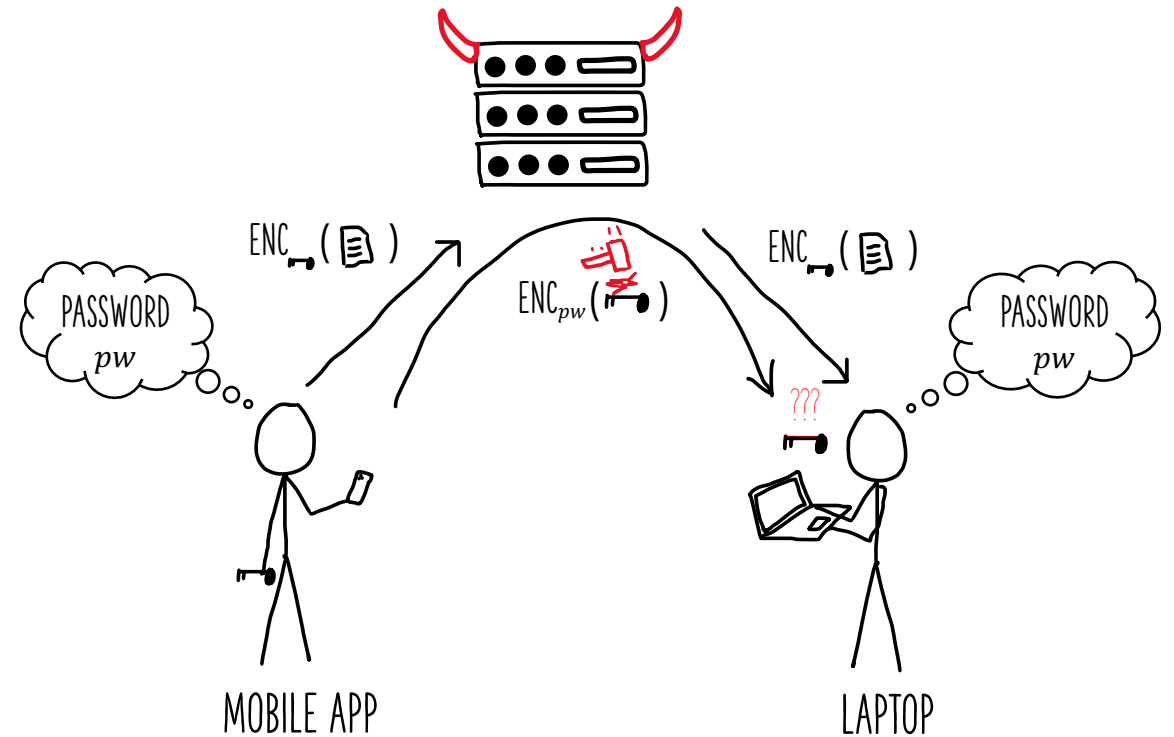
- OneDrive
- Dropbox
- Google Drive
- iCloud Drive

OPTIONAL E2EE AT COST OF FUNCTIONALITY

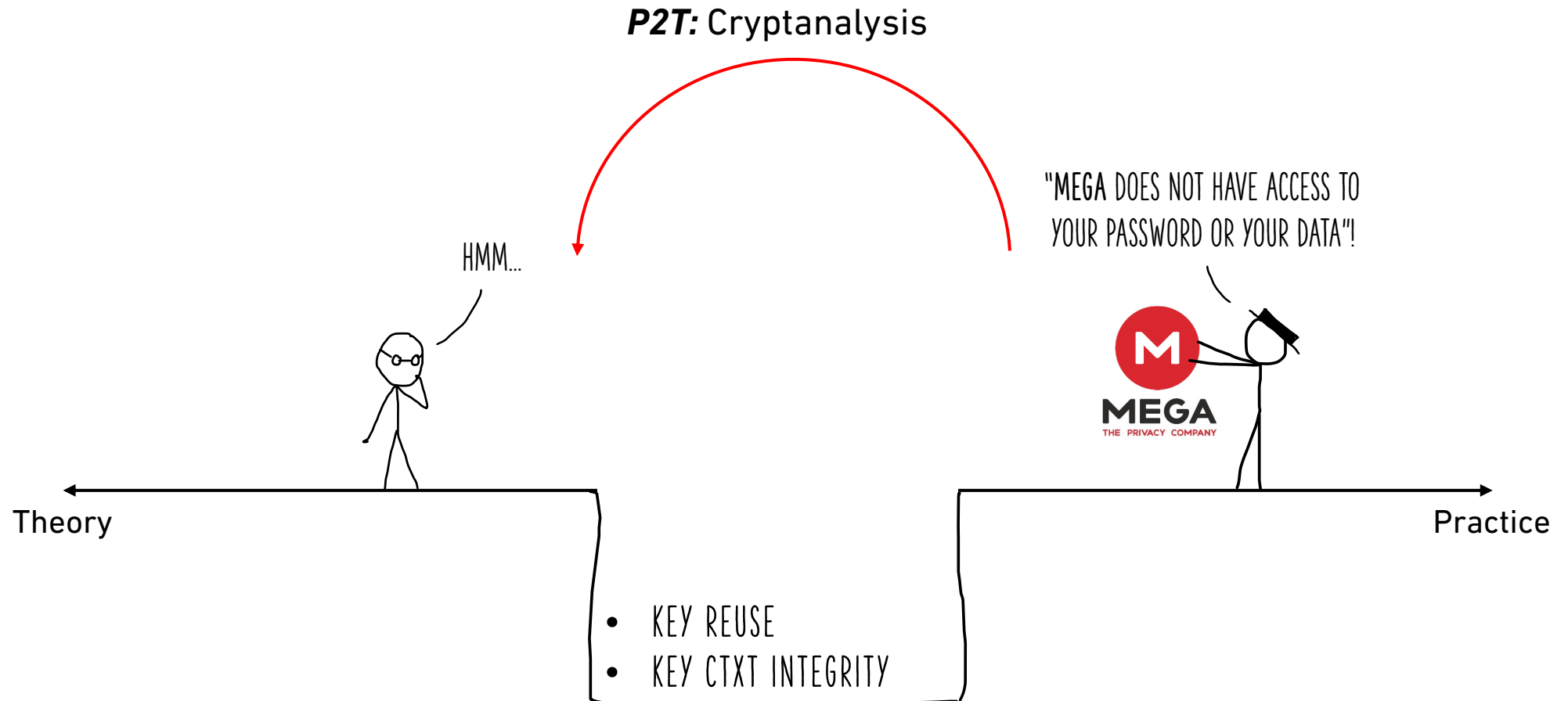


# E2EE Cloud Storage Implementation

- Client-side encryption
  - Pick fresh key to encrypt file
- Issue on download
  - Retrieving key on another device
- Solution
  - Send key encrypted with password over server
- Untrusted server
  - Key overwriting attacks



# P2T Example: The Cryptanalysis of MEGA



# MEGA: Exploiting Authentication for File Decryption\*

\*highly simplified

## Challenge-response authentication

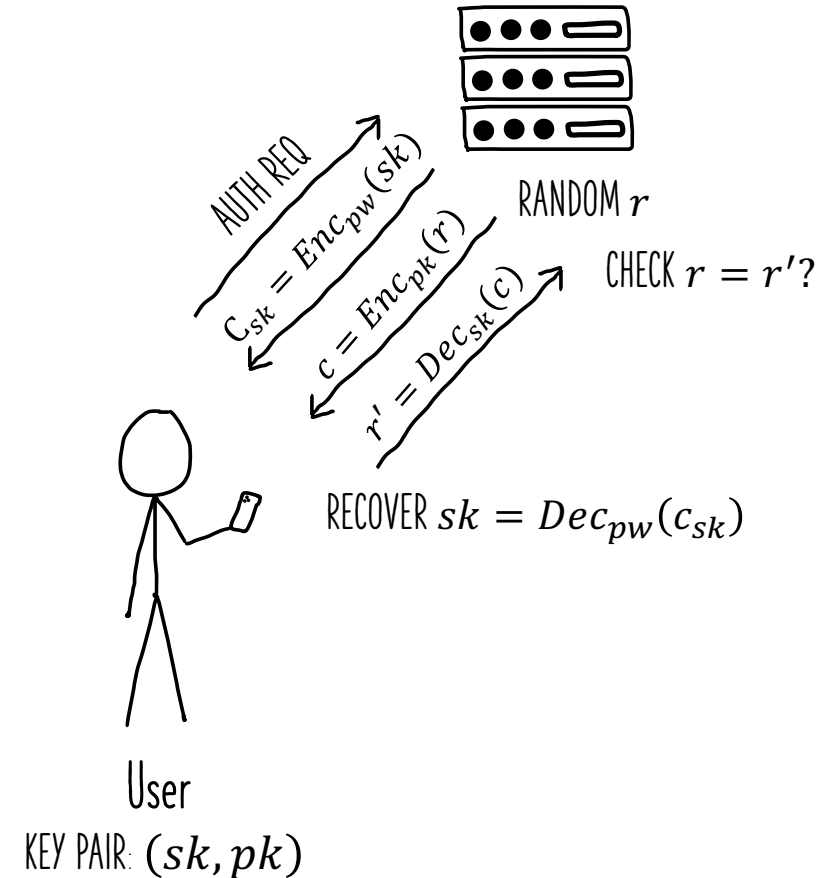
### Server:

- Send secret key  $sk$  encrypted with password  $pw$
- Encrypt challenge  $r$  with user public key  $pk$

### User:

- Decrypt secret key ciphertext  $c_{sk}$  with  $pw$
- Decrypt challenge  $c$ , send recovered  $r'$  back

Authentication successful if  $r = r'$

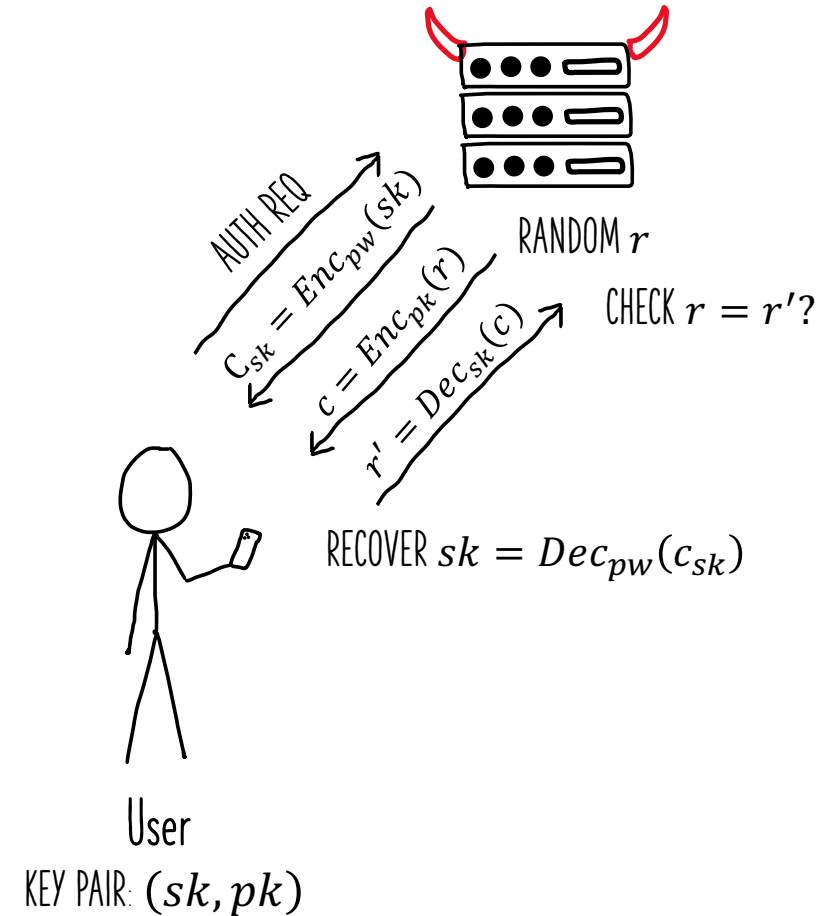


# MEGA: Exploiting Authentication for File Decryption\*

\*highly simplified

## Attack

1. [2] attack to recover file keys  $fk$
2. Key reuse:  $Enc_{pw}(sk)$  and  $Enc_{pw}(fk)$



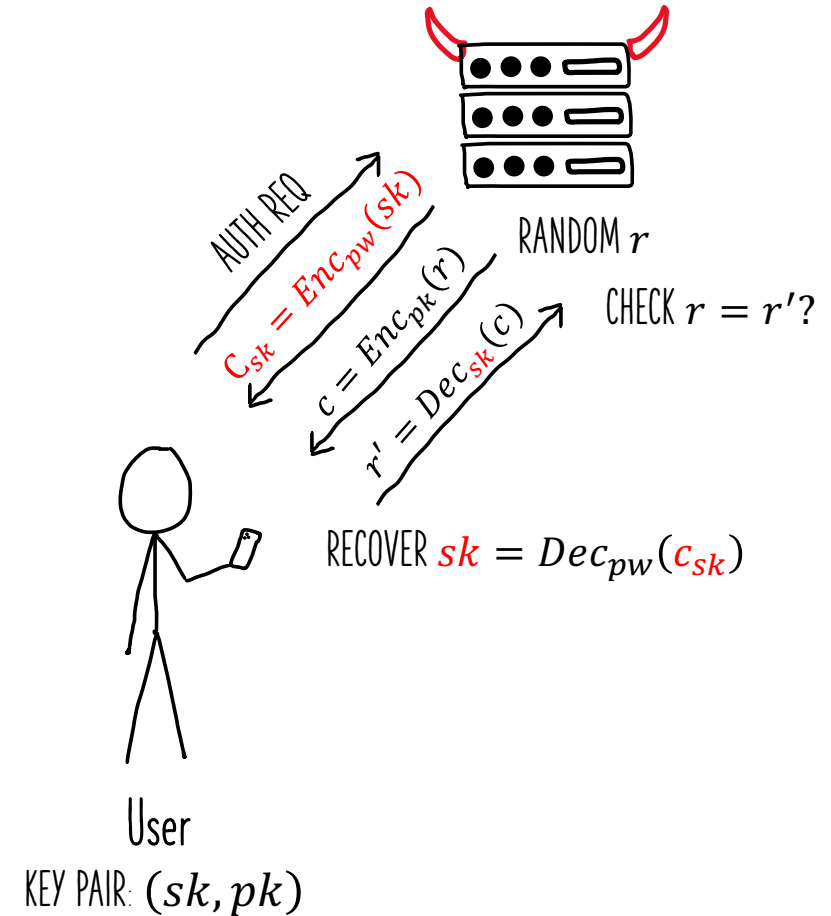
[2] Matilda Backendal, Miro Haller and Kenneth G. Paterson. "MEGA: Malleable Encryption Goes Awry". IEEE S&P 2023.

# MEGA: Exploiting Authentication for File Decryption\*

\*highly simplified

## Attack

1. [2] attack to recover file keys  $fk$
2. Key reuse:  $Enc_{pw}(sk)$  and  $Enc_{pw}(fk)$
3. Partially overwrite  $c_{sk}$  with  $Enc_{pw}(fk)$ 
  - No integrity protection of  $c_{sk}$ !



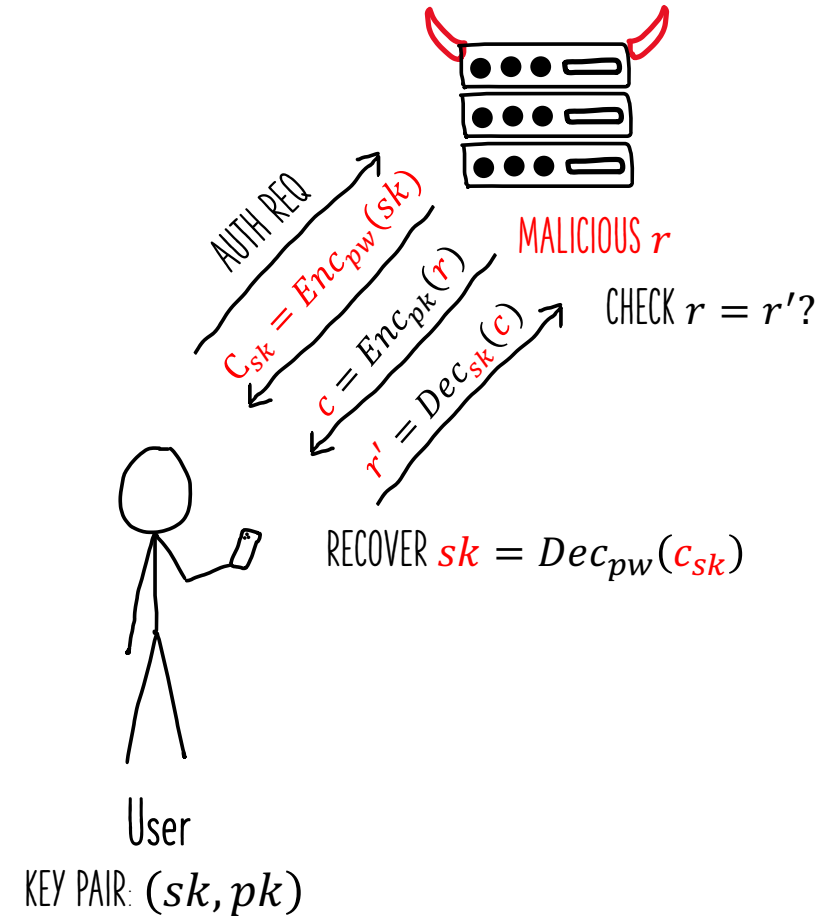
[2] Matilda Backendal, Miro Haller and Kenneth G. Paterson. "MEGA: Malleable Encryption Goes Awry". IEEE S&P 2023.

# MEGA: Exploiting Authentication for File Decryption\*

\*highly simplified

## Attack

1. [2] attack to recover file keys  $fk$
2. Key reuse:  $Enc_{pw}(sk)$  and  $Enc_{pw}(fk)$
3. Partially overwrite  $c_{sk}$  with  $Enc_{pw}(fk)$ 
  - No integrity protection of  $c_{sk}$ !
4. Pick malicious  $r$



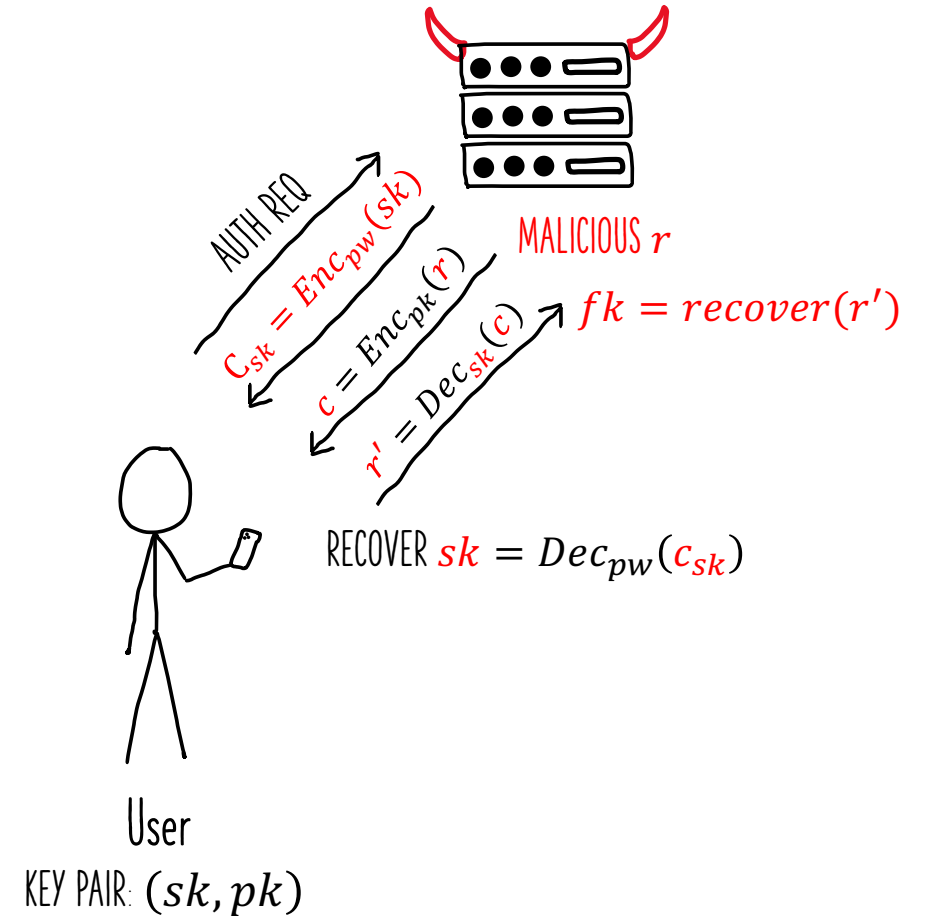
[2] Matilda Backendal, Miro Haller and Kenneth G. Paterson. "MEGA: Malleable Encryption Goes Awry". IEEE S&P 2023.

# MEGA: Exploiting Authentication for File Decryption\*

\*highly simplified

## Attack

1. [2] attack to recover file keys  $fk$
2. Key reuse:  $Enc_{pw}(sk)$  and  $Enc_{pw}(fk)$
3. Partially overwrite  $c_{sk}$  with  $Enc_{pw}(fk)$ 
  - No integrity protection of  $c_{sk}$ !
4. Pick malicious  $r$
5. Recover  $fk$  from  $r'$



[2] Matilda Backendal, Miro Haller and Kenneth G. Paterson. "MEGA: Malleable Encryption Goes Awry". IEEE S&P 2023.

## Challenges & Issues in MEGA

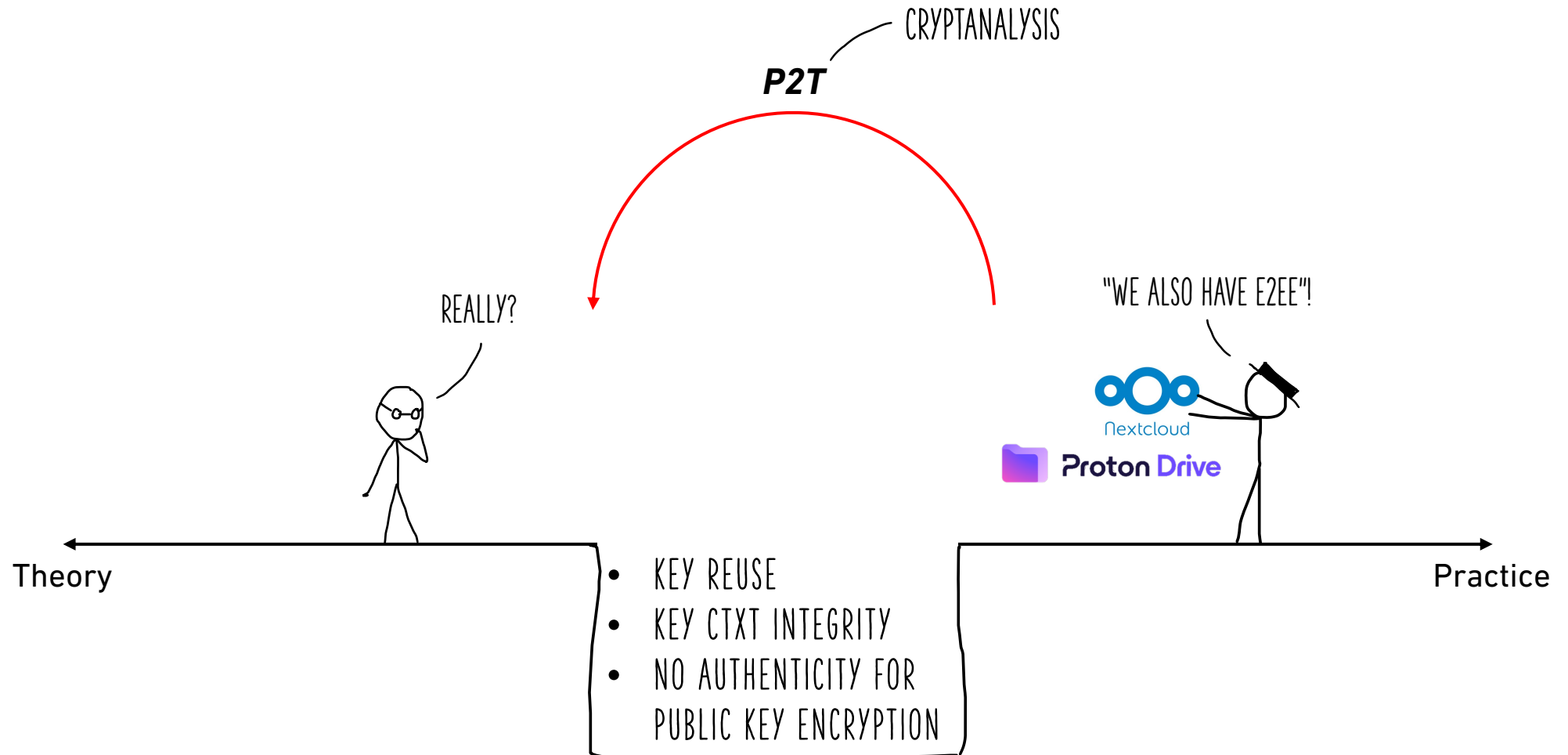
- Integrity for key ciphertexts
- Key reuse
- Patching is hard
  - Re-encryption requires > 185 days
- Multi-device access
- Sharing is tricky

## Lessons Learned

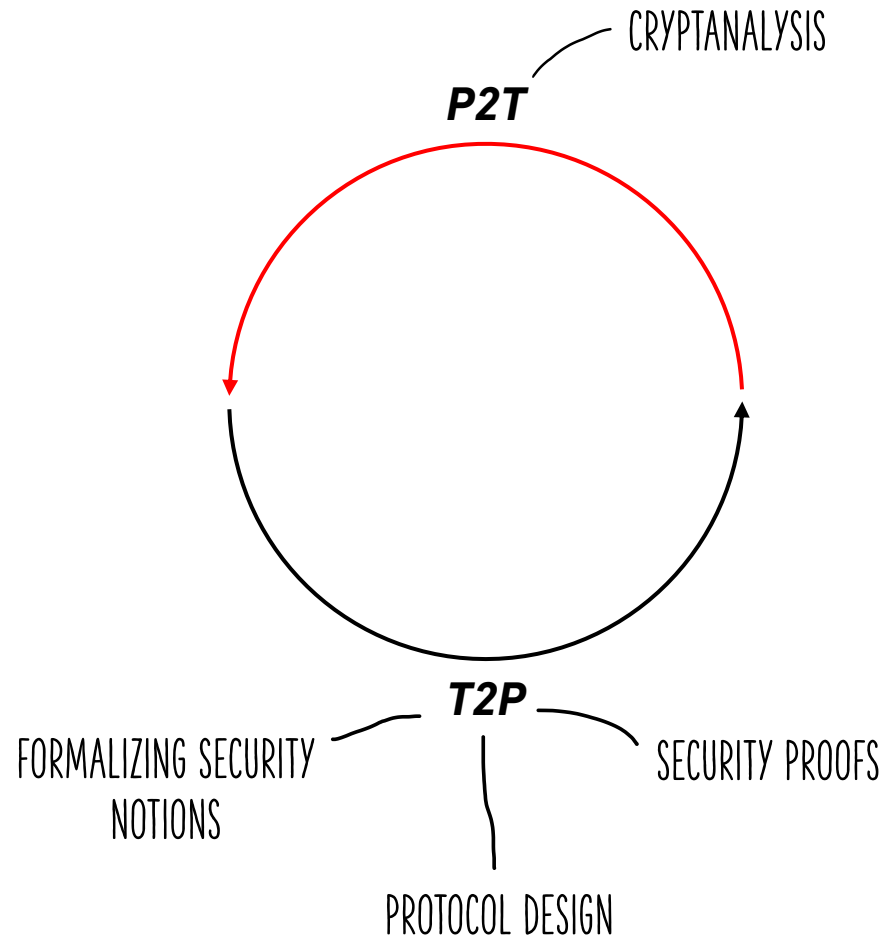
- Unclear security goals
- Key separation is essential
- Cryptographic agility & minimize chance of vulnerabilities
- Password-based security
- Interaction with (potentially malicious) users/server



# The E2EE Cloud Storage Cycle

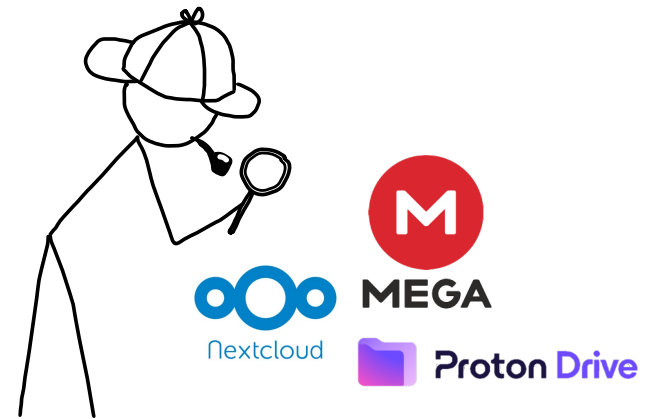


# The E2EE Cloud Storage Cycle



# Security Notions for E2EE Cloud Storage: Operations and Syntax

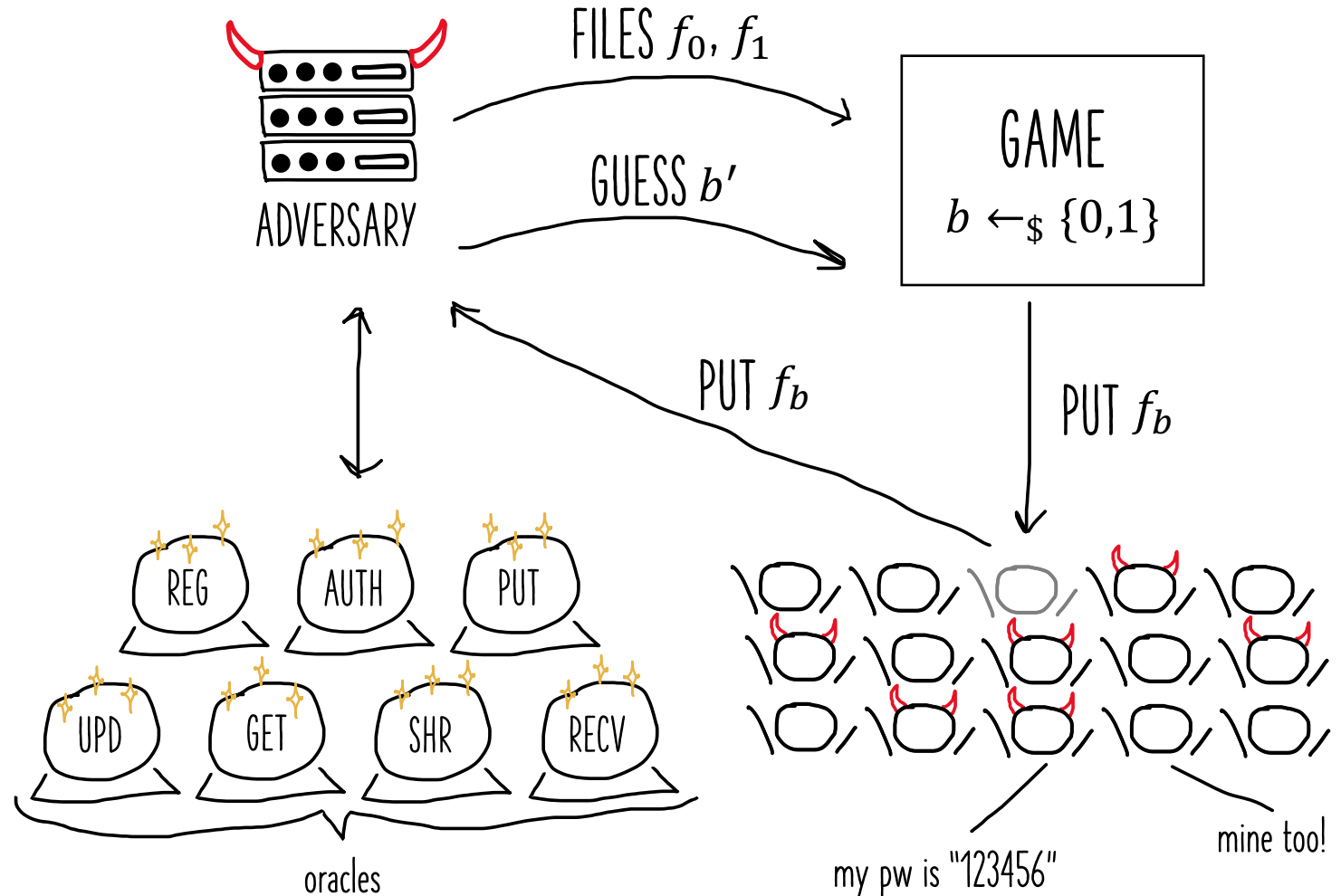
- Identify core functionalities
  - Register (reg)
  - Authenticate (auth)
  - Upload (put)
  - Update (upd)
  - Download (get)
  - Share (shr)
  - Receive (recv)
- Define syntax to express them
  - Non-atomic operations
  - Allow arbitrary interleavings



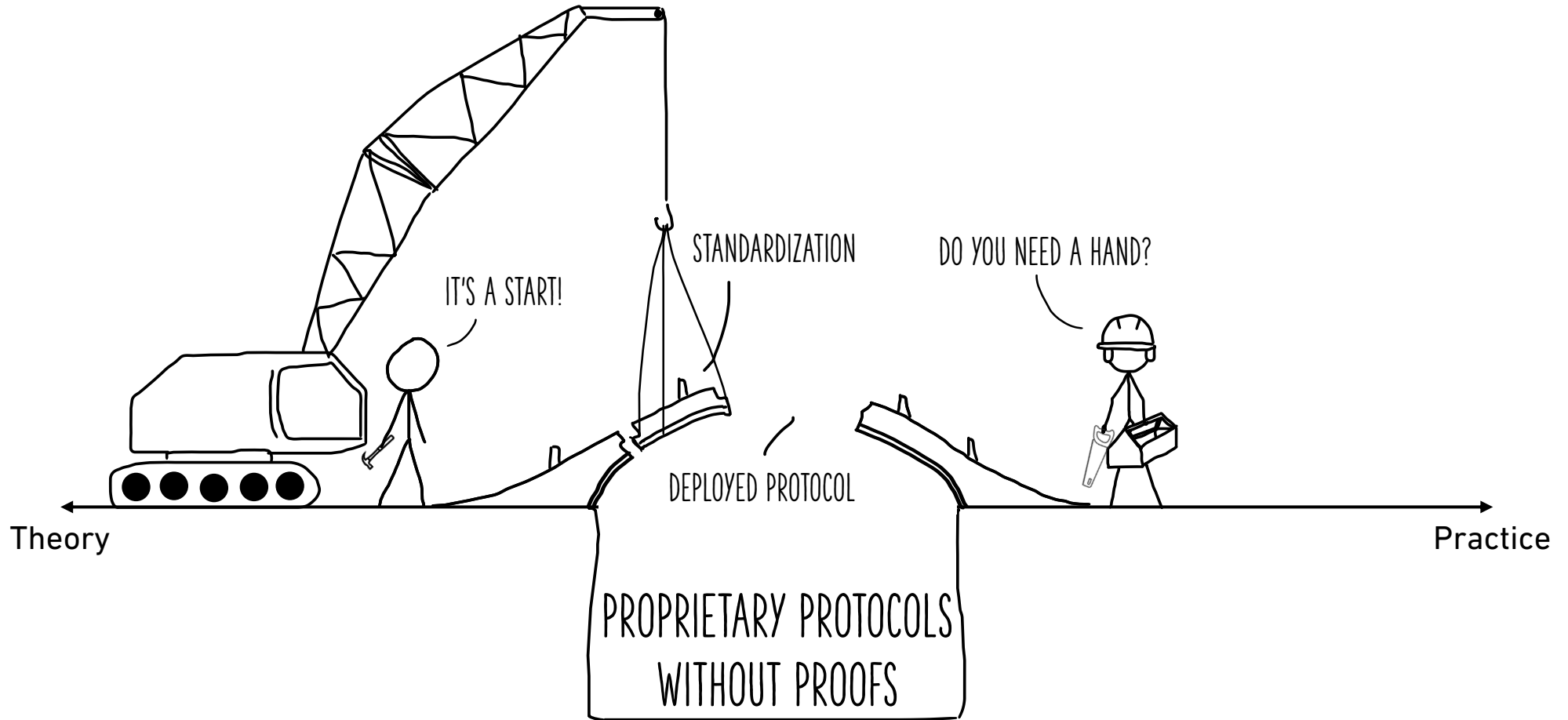
# Security notions for E2EE cloud storage: game

## Security game intuition

- Malicious server (adversary)
- Provide two files  $f_0, f_1$
- File  $f_b$  is uploaded
- Guess bit  $b' = b$
- Full control over state
- Users with correlated pws
- Oracles to make honest users perform actions
- User compromise



# Building a Standard for E2EE Cloud Storage?

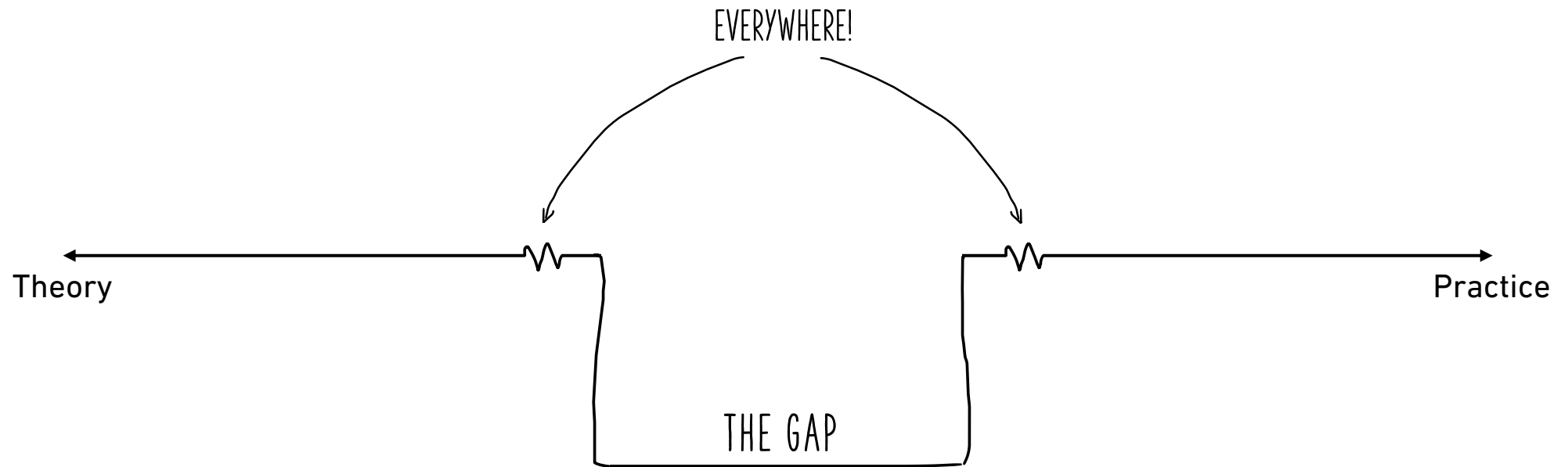


# Conclusion

---

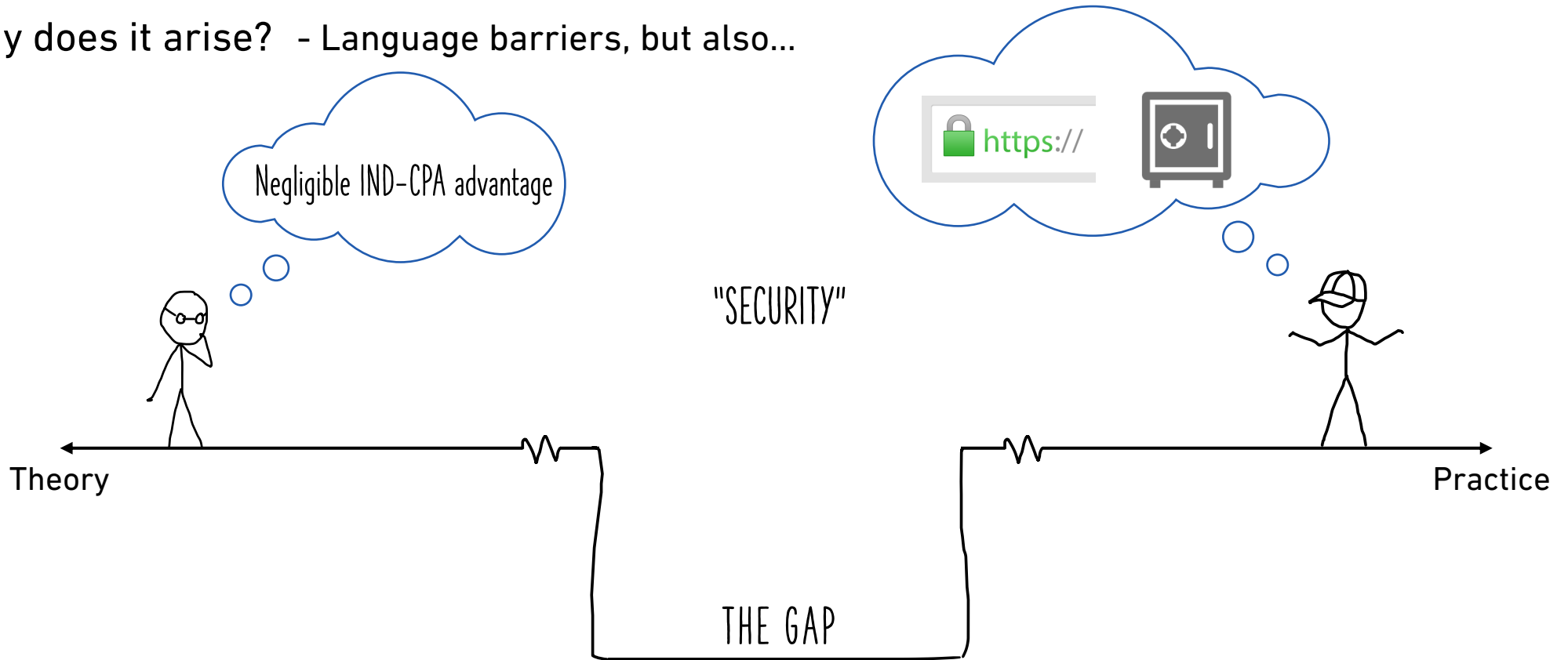
# Conclusion

- Where does the gap arise?



# Conclusion

- Where does the gap arise? - Everywhere
- Why does it arise? - Language barriers, but also...





# Overstatements

WHAT PEOPLE CLAIM THEY BUILT



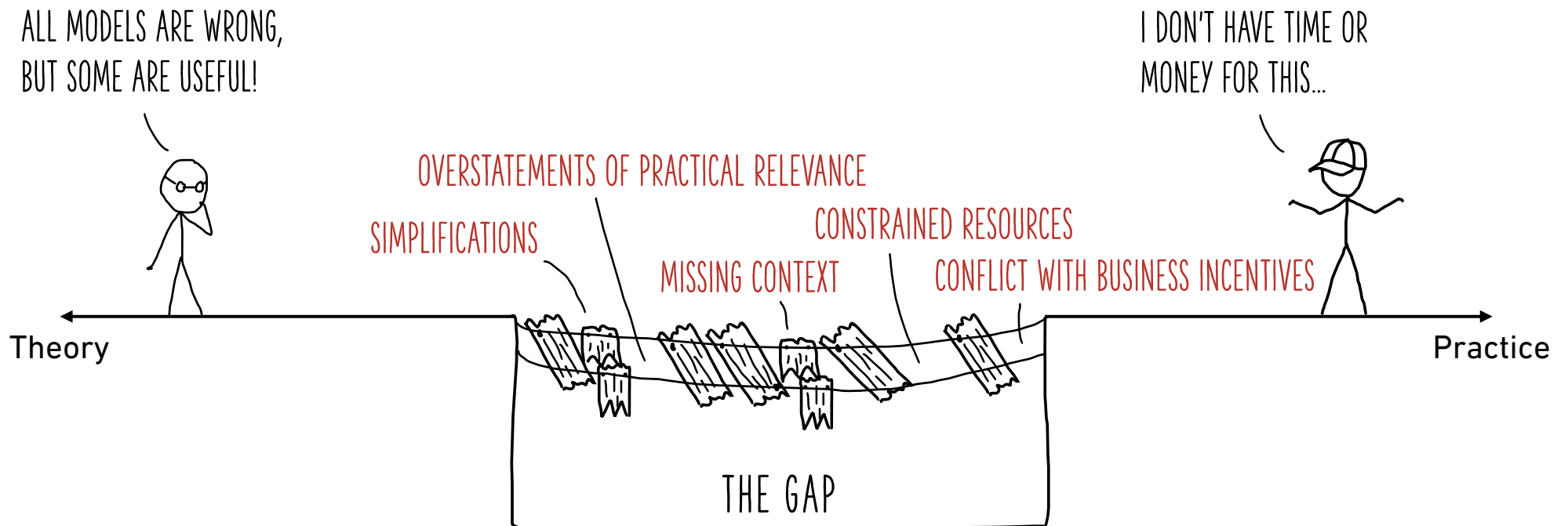
WHAT THEY ACTUALLY BUILT



Image credit: Umer Sayyam, unsplash.com

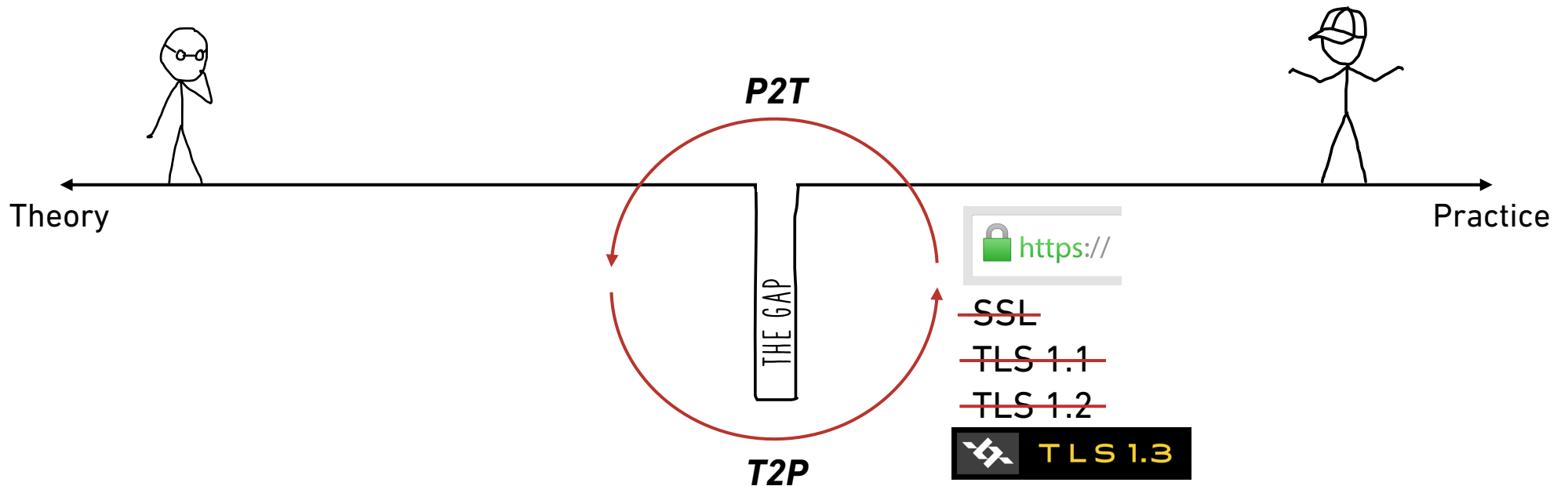
# Conclusion

- Where does the gap arise? - Everywhere
- Why does it arise?

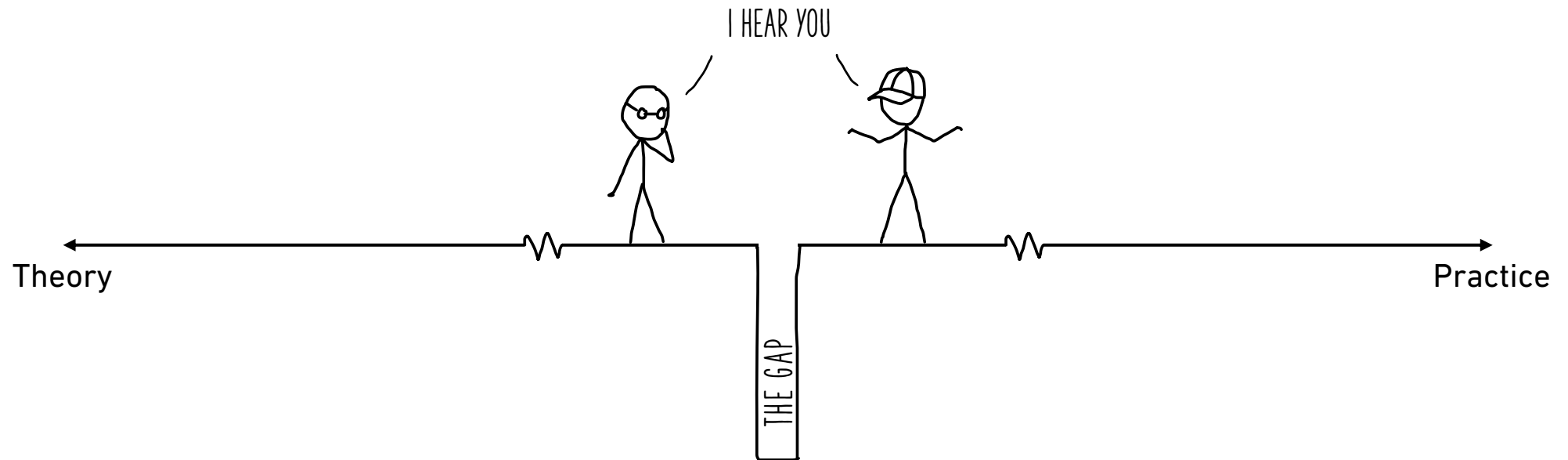


# Conclusion

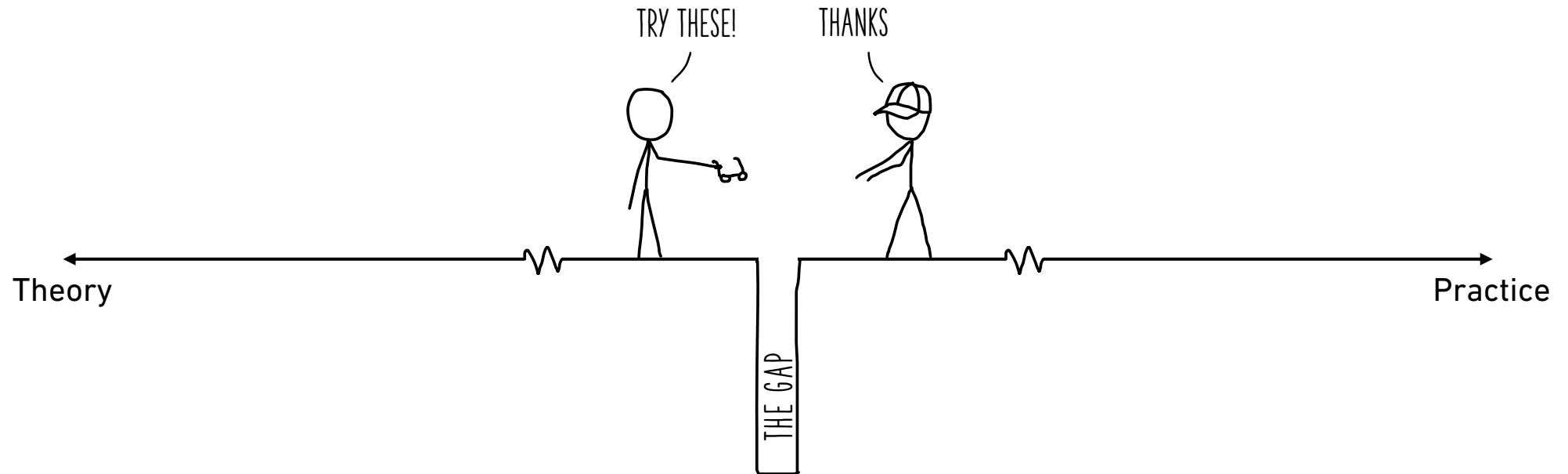
- Where does the gap arise? - Everywhere
- Why does it arise? - It's complicated
- Why is one loop of the cycle not enough to close the gap?



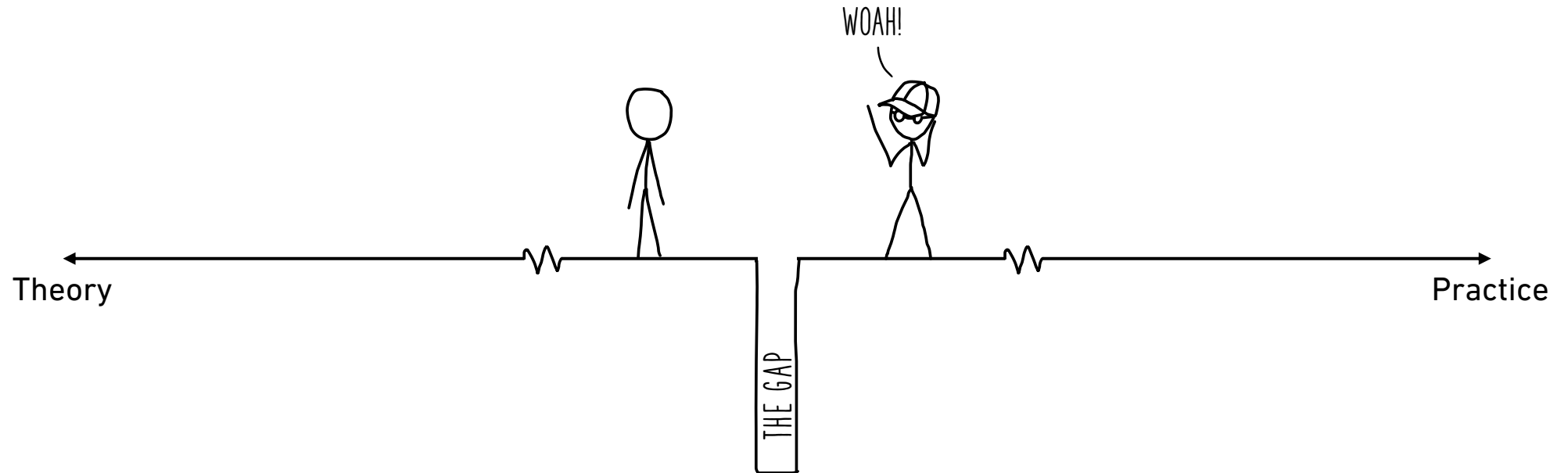
# What Can We Do?



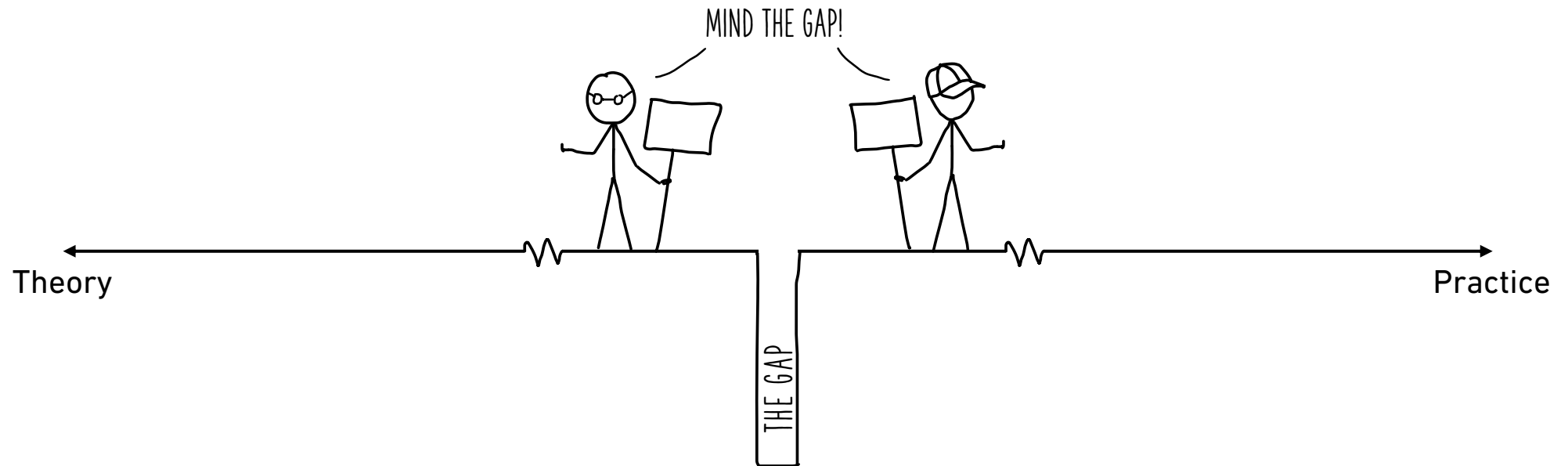
# What Can We Do?



# What Can We Do?



# What Can We Do?



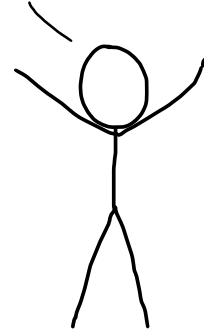
# Why Should You Do Applied Cryptography?

- It's impactful!
- It's profitable!
- It's fun!

caw.cryptanalysis.fun



WHERE DO I SIGN UP?



THANKS!

